$\mathbf{T}_{\text{EMPLE}} \; \mathbf{U}_{\text{NIVERSITY}} \; \mathbf{M}_{\text{ATHEMATICS}} \; \mathbf{C}_{\text{OLLOQUIUM}}$ 

## Nicola Garofalo

Purdue University

will speak on

## Generalized curvature-dimension inequalities, Li-Yau inequalities and volume growth in sub-Riemannian geometry

ABSTRACT: I will discuss some recent joint works with F. Baudoin, with Baudoin and M. Bonnefont, and with Baudoin, Bonnefont and I. Munive. Starting from a generalization of the curvature-dimension inequality, we develop a notion of Ricci lower bound that is appropriate for large classes of sub-Riemannian manifolds, including (CR) Sasakian manifolds and stratified nilpotent Lie groups with step two. In these sub-Riemannian manifolds we prove parabolic inequalities of Li-Yau type, a scale invariant Harnack inequality, Gaussian upper and lower bounds, a global volume doubling estimate, global Poincare' inequalities, and a compactness theorem of Bonnet-Myers type. The lecture will have an expository character.

> Monday, March 12, 2012 Lecture at 4:00 pm Coffee, tea, and refreshments from 3:40 pm Room 617, Wachman Building Department of Mathematics