## $\mathbf{T}_{\text{EMPLE}} \; \mathbf{U}_{\text{NIVERSITY}} \; \mathbf{M}_{\text{ATHEMATICS}} \; \mathbf{C}_{\text{OLLOQUIUM}}$

## Sergei Tabachnikov

Penn State

will speak on

## The mysterious Pentagram Map

ABSTRACT: The pentagram map acts on plane *n*-gons, considered up to projective equivalence, by drawing the diagonals that connect second-nearest vertices and taking the new *n*-gon formed by their intersections; it also acts on more general objects called twisted polygons. Introduced by R. Schwartz about 18 years ago, the pentagram map has quasi-periodic behavior usually encountered in integrable systems. I shall demonstrate that the pentagram map has an invariant Poisson structure, sufficiently many integrals, and is completely integrable in the Arnold-Liouville sense. I shall also explain that the pentagram map is a discretization of the Boussinesq equation, a well known completely integrable PDE. As a byproduct, new configuration theorems of classical projective geometry will be exhibited.

> Monday, 12 October 2009 Lecture at 4:00 pm Coffee, tea, and refreshments from 3-5 pm Room 617, Wachman Building Department of Mathematics