$\mathbf{T}_{\text{EMPLE}} \; \mathbf{U}_{\text{NIVERSITY}} \; \mathbf{M}_{\text{ATHEMATICS}} \; \mathbf{C}_{\text{OLLOQUIUM}}$

Matthew Stover

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will speak on

Ends of hyperbolic manifolds

ABSTRACT: Let M be a compact n-manifold with nonempty boundary consisting of a nonempty disjoint union of tori. Does the interior of Madmit a complete hyperbolic metric of finite volume? When n is 2 or 3, there is a very satisfying answer depending only on the topology of M. In higher dimensions we know very little. For example, we do not know a single example of a 1-ended complete hyperbolic n-manifold of finite volume for any n > 3. The only known constructions in high dimensions are either arithmetic or hybrids of arithmetic manifolds. I will explain why 1-cusped arithmetic hyperbolic manifolds do not exist for any n > 29. This follows from a much stronger finiteness theorem, namely that for every k > 0, the arithmetic negatively curved locally symmetric spaces with k ends fall into finitely many commensurability classes.

> Monday, January 28, 2013 Lecture at 4:00 pm Coffee, tea, and refreshments from 3:30 pm Room 617, Wachman Building Department of Mathematics