Temple University Mathematics Colloquium

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will speak on

The Associative Law in Multary Quasigroups

A multary (or *n*-ary) quasigroup is a set with a multary operation, $f: Q^n \to Q$, such that, given any *n* of the variables in the expression $f(x_1, ..., x_n) = x_0$, the last variable is uniquely determined. Such an operation is like a group operation but with many arguments and without an analog of associativity. Multary quasigroups were introduced by Belousov and Sandik in 1966, coming from the viewpoint of universal algebra.

A basic question is whether a given f is essentially *n*-ary or is compounded of smaller multary quasigroups. This is a kind of associativity or factorization. For instance, one way to construct a multary quasigroup is to iterate a (binary) group operation. An iterated group has all possible factorizations, and a result of Belousov and his school was that, if f has all possible factorizations, then it is essentially an iterated group.

In general, f has a graph of factorizations, G(f), which may not be the complete graph. Belousov conjectured that, if G(f) is 3connected, then it is complete. I will outline a proof based on the theory of biased expansion graphs. (A biased expansion of a graph is a kind of branched covering graph.) $\mathbf{2}$

Monday, March 21, 2005 Lecture at 4:00 PM (\$) Coffee, tea, and refreshments from 3-5 PM. Room 617, Wachman Building Department of Mathematics