$\mathbf{T}_{\text{EMPLE}} \; \mathbf{U}_{\text{NIVERSITY}} \; \mathbf{M}_{\text{ATHEMATICS}} \; \mathbf{C}_{\text{OLLOQUIUM}}$

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will speak on

The polynomial van der Waerden theorem

ABSTRACT: The classical van der Waerden theorem is a result about the existence of arithmetic progressions in sets; it can be stated as follows: Given a *c*-coloring COL of \mathbb{Z} (i.e., a partition of \mathbb{Z} into *c* disjoint subsets) and a positive integer *k*, there exists $a, d \in \mathbb{Z}$ with $d \neq 0$ such that $COL(a) = COL(a + d) = COL(a + 2d) = \cdots = COL(a + kd)$. The polynomial van der Waerden theorem, proven by Bergelson and Leibman, is a generalization which uses polynomials in *d* instead of the linear polynomials $d, 2d, \ldots, kd$.

The original proof of the polynomial van der Waerden theorem involved ergodic techniques and was somewhat difficult. Subsequently, an elementary proof was given by Walters. We will present a simpler version of his proof and discuss even further generalizations.

> Monday, October 23, 2006 Lecture at 4:00 PM (#) Coffee, tea, and refreshments from 3-5 PM. Room 617, Wachman Building Department of Mathematics