TEMPLE UNIVERSITY

Department of Mathematics

Analysis Seminar

Room 617 Wachman Hall

Monday, September 15, 2014, 2:40 p.m.

Eigenspace decomposition of the kernel of \mathbb{R} -invariant operators

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Let \mathcal{T} be a smooth nowhere vanishing vector field on a closed manifold M and P a second order differential operator on M commuting with P and such that $P - \mathcal{T}^2$ is elliptic. Then \mathcal{T} can be viewed as acting as an unbounded operator on the kernel of P in L^2 , giving as such (under certain circumstances), a selfadjoint operator with discrete spectrum. Further, assuming regularity properties for the solutions u of Pu = f in terms of those of f, one obtains results about whether the spectrum of \mathcal{T} (a subset of \mathbb{R}) is bounded from below (or from above). I will explain how one proves these results and then describe interesting applications in complex and CR geometry.