## **ALGEBRA SEMINAR**

## A Deformation Complex for Modules over Deformation Quantization

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ABSTRACT: For a smooth affine variety, X, A. Yekutieli proved, following the seminal work of M. Kontsevich, that formal associative deformations of  $\mathcal{O}_X$  up to equivalence are in bijection with formal Poisson structures on X up to equivalence. Fixing a deformation quantization of  $\mathcal{O}_X$ , which we denote by  $\mathcal{A}$ , a natural problem is then to see which  $\mathcal{O}_X$ modules can be deformed to  $\mathcal{A}$ -modules. We will construct a curved dg Lie algebra which controls deformations of  $\mathcal{O}_X$ -modules to  $\mathcal{A}$ -modules. We will then discuss first and second order deformations of modules which are locally free and supported on a smooth subvariety. If time permits we will discuss a possible solution for formal deformations of modules. Part of this work is joint with Vladimir Baranovsky and Victor Ginzburg.

> Monday, September 26, 2011 1:40 – 2:30 pm Room 617, Wachman Hall Department of Mathematics